

Algebraic

- $a^2 - b^2 = (a - b)(a + b)$
- $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$
- Quadratic Formula: $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Geometric

- Area of Circle: πr^2
- Circumference of Circle: $2\pi r$
- Circle with center (h, k) and radius r :

$$(x - h)^2 + (y - k)^2 = r^2$$
- Distance from (x_1, y_1) to (x_2, y_2) :

$$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

- Area of Triangle: $\frac{1}{2}bh$
- $\sin \theta = \frac{\text{opposite leg}}{\text{hypotenuse}}$
- $\cos \theta = \frac{\text{adjacent leg}}{\text{hypotenuse}}$
- $\tan \theta = \frac{\text{opposite leg}}{\text{adjacent leg}}$
- If $\triangle ABC$ is similar to $\triangle DEF$ then

$$\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$$

- Volume of Sphere: $\frac{4}{3}\pi r^3$
- Surface Area of Sphere: $4\pi r^2$
- Volume of Cylinder/Prism: (height)(area of base)
- Volume of Cone/Pyramid: $\frac{1}{3}(\text{height})(\text{area of base})$

Theorems

- (IVT) If f is continuous on $[a, b]$, $f(a) \neq f(b)$, and N is between $f(a)$ and $f(b)$ then there exists $c \in (a, b)$ that satisfies $f(c) = N$.

Derivative Formulas:

$$(x^n)' = n \cdot x^{n-1}, \quad (c)' = 0, \quad (mx+b)' = m$$

$$[f(x)g(x)]' = f'(x)g(x) + f(x)g'(x);$$

$$\left[\frac{f(x)}{g(x)}\right]' = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Limits

- $\lim_{x \rightarrow a} f(x)$ exists if and only if $\lim_{x \rightarrow a^-} f(x) = \lim_{x \rightarrow a^+} f(x)$
- $\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$
- $\lim_{\theta \rightarrow 0} \frac{1 - \cos \theta}{\theta} = 0$

Derivatives

- $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$
- $(\cot x)' = -\csc^2 x$
- $(\csc x)' = -\csc x \cdot \cot x$

Trigonometric

- $\sin^2 \theta + \cos^2 \theta = 1$
- $\sin(2\theta) = 2 \sin \theta \cos \theta$
- $\cos(2\theta) = \cos^2 \theta - \sin^2 \theta$
 $= 1 - 2 \sin^2 \theta$
 $= 2 \cos^2 \theta - 1$

- Table of Trig Values

x	0	$\pi/6$	$\pi/4$	$\pi/3$	$\pi/2$
$\sin(x)$	0	$1/2$	$\sqrt{2}/2$	$\sqrt{3}/2$	1
$\cos(x)$	1	$\sqrt{3}/2$	$\sqrt{2}/2$	$1/2$	0
$\tan(x)$	0	$\sqrt{3}/3$	1	$\sqrt{3}$	DNE

Trigonometric Derivative

$$(\sin x)' = \cos x, \quad (\tan x)' = \sec^2 x \\ (\cos x)' = -\sin x, \quad (\sec x)' = \tan x \cdot \sec x.$$

Average Rate of Change of $f(x)$ over $[a, b]$

$$= \frac{f(b) - f(a)}{b - a}$$

Law of Motion:

$$v(t) = s'(t), \quad a(t) = v'(t) = s''(t)$$