# STT 456 Review Problems for Final Exams <br> Thursday, April 29, 2015 <br> 5-8 pm, Room C-304 

1. You are given:

- Mortality follows the Illustrative Life Table.
- All lives are independent.
- Deaths are uniformly distributed over each year of age.

Evaluate $q_{50: 55: 60}^{1}$
2. For a fully discrete whole life insurance of $\$ 1$ issued to (40), you are given:

- $P$ is the annual benefit premium determined according to the equivalence principle.
- $P^{*}$ is the smallest possible annual benefit premium to ensure that the probability of a positive loss-at-issue is less than 0.50 .

You are given:

- Mortality follows the Illustrative Life Table.
- $i=6 \%$

Calculate $\frac{P}{P^{*}}$.
3. For a special whole life insurance on (45), you are given:

- Benefit is paid at the end of the year of death. The death benefit is $\$ 100,000$ for the first 20 years and reduces to $\$ 50,000$ thereafter.
- The annual benefit premium of $\$ 4,945$ is payable once at the beginning of each year for the first 20 years only; no premiums are payable after 20 years.
- The following actuarial present values:

| $x$ | $A_{x}$ | $\ddot{a}_{x}$ | ${ }_{10} E_{x}$ |
| :---: | :---: | :---: | :---: |
| 55 | 0.5628 | 4.8091 | 0.0758 |
| 65 | 0.7532 | 2.7147 | 0.0015 |

Calculate the benefit reserve at the end of 10 years.
4. For a double decrement table, you are given:

- $q_{x}^{\prime(1)}=0.1$
- $q_{x}^{(2)}=0.2$
- Each decrement is uniformly distributed over each year of age in its associated single decrement table.

Calculate $q_{x}^{(1)}$.
5. Patients are classified as Sick (S), Critical (C), or Discharged (D). Transition occur according to the following transition matrix:

$$
\begin{aligned}
& \\
& \mathrm{S} \\
& \mathrm{C} \\
& \mathrm{D}
\end{aligned}\left(\begin{array}{ccc}
\mathrm{S} & \mathrm{C} & \mathrm{D} \\
0.60 & 0.20 & 0.20 \\
0.10 & 0.50 & 0.40 \\
0.00 & 0.00 & 1.00
\end{array}\right)
$$

Calculate the probability that a patient who is classified as Sick today will be classified as Sick three days later.
6. An insurance company uses the following "accidental death" model:


For a special whole life insurance policy issued to a life $(x)$, you are given:

- A benefit of $\$ 4$ is payable at the moment of death of $(x)$ if death is due to acidental causes; otherwise, the benefit is only $\$ 1$.
- Transition intensities are

$$
\mu_{x+t}^{01}=0.005 \text { and } \mu_{x+t}^{02}=0.010, \text { for all } t>0
$$

- $\delta=4 \%$

Calculate the actuarial present value of the benefits provided by this policy.
7. For a Universal Life policy issued to (50) with death benefit equal to $\$ 10,000$ plus the account value, you are given:

- Premiums are deposited at the start of each year.
- The expense charge in each year is $2.5 \%$ of premium. There are no other expense charges.
- The cost of insurance rate each year is equal to $150 \%$ of the applicable mortality rate at the attained age.
- $i^{c}=i^{q}=5 \%$ for all years
- The account value at the end of 5 years is $\$ 11,196.12$.
- $q_{55}=0.002$
- The corridor factor requirement is a minimum of 1.5 each year.

Calculate the largest amount of premium this policyholder can pay at the beginning of the sixth year.
8. For a Type A universal life policy issued to (50), you are given:

- The face amount is 100,000 .
- All cash flows occur at policy anniversaries.
- The policyholder pays an initial premium of 15,000 .
- The cost of insurance (COI) is calculated based on $120 \%$ of the mortality in the Illustrative Life Table. The interest rate for discounting the net amount at risk, $i^{q}$, is 0.04 .
- The expense charge is $1 \%$ of premium.
- The credited interest rate for policy year 1 is $5 \%$.
- The corridor factor in year 1 is 2.2 .
- The surrender charge in policy year 1 is $5 \%$ of the premium paid.
(a) Calculate the COI in policy year 1 assuming there is no corridor factor requirement.
(b) Calculate the COI in policy year 1 based only on the corridor factor (as if the face amount were 0 ).
(c) Determine the COI in policy year 1 .

9. For a Type B universal life policy of 200,000 issued to (55):

- A premium of 5000 is paid at the start of the ninth year.
- Expense charges are $35 \%$ of first year premiums and $10 \%$ of renewal premiums.
- The cost of insurance in the ninth year is based on $q_{63}=0.01$. Death benefits are assumed to be paid at the end of the year.
- The account values at the beginning and end of the ninth year are 45,000 and 49,480 , respectively.
- The interest rate used to discount the COI is equal to the interest credited, $i^{c}$, during the ninth year.


## Calculate $i^{c}$.

10. For two universal life policies issued to (60): Policy 1 is a Type A universal life with death benefit of 100,000 while Policy 2 is a Type B universal life with death benefit of 100,000 . For each policy:

- Death benefits are paid at the end of the month of death.
- Account values are calculated monthly.
- Level monthly premiums of $G$ are payable at the beginning of each month. Past premiums may have been different from $G$, and may not have been the same for both policies.
- Mortality rates for calculating COI follows the Illustrative Life Table, with the UDD assumption for fractional ages.
- Interest is credited at a monthly effective rate of 0.004 .
- The interest rate used for accumulating and discounting in the COI calculation is a monthly effective rate of 0.004 .
- Level expense charges of $E$ are deducted at the beginning of each month.

At the end of the 36th month, the account value for Policy 1 equals the account value for Policy 2.
Calculate the ratio of the account value for Policy 1 at the end of the 37 th month to the account value of Policy 2 at the end of the 37 th month.
11. For a universal life policy with a death benefit of 10,000 plus the account value on (60), you are given:

- The following table of values:

| Month | Monthly <br> Premium | Percent of <br> Premium <br> Charge | Monthly Cost <br> of Insurance <br> Rate per 1000 | Monthly <br> Expense <br> Charges | Surrender <br> Charge |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | 100 | $15 \%$ | 3.00 | 10 | 400 |

- The credited interest rate is $i^{(12)}=0.048$.
- The account value at the end of month 11 is 1500 .

The policy is surrendered at the end of month 12 . The cash surrender value is used as a single premium to purchase a whole life annuity-due whose first 10 annual payments are guaranteed. For this annuity, you are given:

- Mortality follows the Illustrative Life Table.
- $i=0.06$
- The annuity is priced using the equivalence principle.

Calculate the amount of the annual annuity payment.

