

Exercise 3.4

$$(a) \quad {}_2p_{[72]} = p_{[72]} \cdot p_{[72]+1} = (1 - q_{[72]})(1 - q_{[72]+1}) = (1 - 0.005236)(1 - 0.007456) = 0.987347$$

$$(b) \quad {}_3q_{[73]+2} = 1 - {}_3p_{[73]+2} = \underbrace{1 - (1 - q_{[73]+1})(1 - q_{[73]+3})(1 - q_{[73]+4})}_{1 - (1 - 0.011370)(1 - 0.014988)(1 - 0.019316)} = 0.04499775$$

$$(c) \quad {}_1|q_{[65]+4} = (1 - q_{[65]+4}) \cdot q_{70} = (1 - 0.007994)0.010599 = 0.01051427$$

(d) We have

$$\begin{aligned} {}_7p_{[70]} &= p_{[70]} \cdot p_{[70]+1} \cdot p_{[70]+2} \cdot p_{[70]+3} \cdot p_{[70]+4} \cdot p_{75} \cdot p_{76} \\ &= (1 - q_{[70]})(1 - q_{[70]+1})(1 - q_{[70]+2})(1 - q_{[70]+3})(1 - q_{[70]+4})(1 - q_{75})(1 - q_{76}) \\ &= (1 - 0.004285)(1 - 0.005967)(1 - 0.008066)(1 - 0.010629)(1 - 0.013698) \\ &\quad \times (1 - 0.018774)(1 - 0.021053) \\ &= 0.9202714. \end{aligned}$$