Name: \_\_\_\_\_\_ Math 415, Summer II 2013 Quiz #5 (Take-home): Due 08–14–13, 5PM.

For each of the following questions, precisely state an argument justifying your reasoning. You may *discuss* these problems with other students in the class only. Each write-up should be in your own words and written *by yourself*.

**1.** Fit a linear function of the form,  $p(t) = c_0 + c_1 t$  to the data points (0,3), (1,3), (1,6) using least squares. Sketch your solution.

**2.** Consider the space  $\mathbb{R}_1[t]$  of polynomials of degree at most one. Define an inner product on this space by

$$\langle f|g \rangle := rac{1}{2} \left( f(0)g(0) + f(1)g(1) \right).$$

Find an orthonormal basis for this inner product space.

**3.** Suppose  $\mathcal{B} = {\mathbf{b}_1, \dots, \mathbf{b}_m}$  is a collection of non-zero orthogonal vectors in an inner product space V. Show that  $\mathcal{B}$  is linearly independent. Show, by example, that the converse is not true.