## Quadric Surfaces

| Surface | Equation | Surface | Equation |
| :---: | :---: | :---: | :---: |
| Ellipsoid | $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}+\frac{z^{2}}{c^{2}}=1$ <br> All traces are ellipses. <br> If $a=b=c$, the ellipsoid is a sphere. | Cone | $\frac{z^{2}}{c^{2}}=\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}$ <br> Horizontal traces are ellipses. <br> Vertical traces in the planes $x=k$ and $y=k$ are hyperbolas if $k \neq 0$ but are pairs of lines if $k=0$. |
| Elliptic Paraboloid | $\frac{z}{c}=\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}$ <br> Horizontal traces are ellipses. <br> Vertical traces are parabolas. <br> The variable raised to the first power indicates the axis of the paraboloid. | Hyperboloid of One Sheet | $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}-\frac{z^{2}}{c^{2}}=1$ <br> Horizontal traces are ellipses. <br> Vertical traces are hyperbolas. <br> The axis of symmetry corresponds to the variable whose coefficient is negative. |
| Hyperbolic Paraboloid | $\frac{z}{c}=\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}$ <br> Horizontal traces are hyperbolas. <br> Vertical traces are parabolas. The case where $c<0$ is illustrated. | Hyperboloid of Two Sheets | $-\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}+\frac{z^{2}}{c^{2}}=1$ <br> Horizontal traces in $z=k$ are ellipses if $k>c$ or $k<-c$. <br> Vertical traces are hyperbolas. <br> The two minus signs indicate two sheets. |

## Vector-valued Functions and Curves

For a vector function $\vec{r}(t)=\langle x(t), y(t), z(t)\rangle$ :

- $\lim _{t \rightarrow c} \vec{r}(t)=\left\langle\lim _{t \rightarrow c} x(t), \lim _{t \rightarrow c} y(t), \lim _{t \rightarrow c} z(t)\right\rangle$.
- $\vec{r}(t)$ is continuous at $t=c$ if $x(t), y(t)$ and $z(t)$ are all continuous at $t=c$.


## Helix

The helix is parameterized by the vector function:
$\vec{r}(t)=\langle\cos (t), \sin (t), t\rangle$


