Name:

Card #: ____

Clear your desk of everything excepts pens, pencils and erasers. Show all your work. If you have a question raise your hand and I will come to you.

- 1. Sketch the graph of $f(x) = x \sin(-x)$ on the interval $[-2\pi, 2\pi]$ by following the below steps.
 - (a) (1 point) Determine if there are any asymptotes or if f is even/odd.
 Solution: f is odd, since f(-x) = -x sin(x) = -x + sin(-x) = -f(x).
 - (b) (2 points) Determine where f is increasing, decreasing, and where any local extrema are.Solution: Use the first derivative test:

$$f'(x) = 1 + \cos(-x)$$

Never undefined. So find when 0 to locate crit. pts.

$$0 = 1 + \cos(-x)$$

$$-1 = \cos(-x)$$

$$x = \{-\pi, \pi\}$$
 (On the interval $[-2\pi, 2\pi]$)

Now we plot and take test points to see:

f is increasing on $[-2\pi, 2\pi]$, never decreasing, and has no local extrema.

(c) (2 points) Determine where f is concave up, concave down, and where any inflection points are.Solution: Lets look at the second derivative:

$$f''(x) = \sin(-x)$$

Never undefined. So find when 0 to locate potential inflection pts.

$$0 = \sin(-x) x = \{-2\pi, -\pi, 0, \pi, 2\pi\}$$
 (On the interval $[-2\pi, 2\pi]$)

Now we plot and take test points to see:

f is concave down on $(-2\pi, -\pi) \cup (0, \pi)$ and is concave up on $(-\pi, 0) \cup (\pi, 2\pi)$. Giving inflection points at $x = \{-\pi, 0, \pi\}$.

(d) (2 points) Sketch f on the graph below. Mark all local extrema and inflection points, if any.Solution:


