

Math 21C-2 Review Sheet

- Sequences

 - Definition

 - Convergence, Limits, Divergence to Infinity

 - ¹ Definition of Convergence

 - Calculation of Limits

 - Nondecreasing Sequence Theorem

- Series

 - Definition of n th Term, Partial Sum, Convergence

 - Geometric Series

 - Techniques for Checking Convergence

 - n th Term Test for Divergence

 - Integral Test

 - Comparison, Limit Comparison Tests

 - Ratio and Root Tests

 - Alternating Series

 - Definitions of Absolute/Conditional Convergence

 - Power Series

 - Definition, Radius of Convergence, Interval of Convergence

 - Term-by-term Differentiation/Integration

 - Taylor and Maclaurin Series

 - Definition

 - Calculation of Taylor series

 - Taylor Polynomials

 - ¹ Remainder Estimation Theorem

- Vectors
 - Rectangular coordinates
 - Distance formula
 - Component form for vectors
 - Magnitude
 - Unit Vectors
 - Vector Addition, Subtraction, Scalar Multiplication
 - Standard Unit Vectors $\vec{i}, \vec{j}, \vec{k}$
 - Dot Product
 - Calculation
 - Angle Formula
 - Orthogonality
 - Projection
 - Cross Product
 - Definition
 - Calculation
 - Geometric Interpretation
 - Equations of Lines in Space
 - Equations of Planes in Space
 - ¹ Distances from Points to Lines/Planes
- Vector-Valued Functions
 - Geometric Interpretation
 - Limits and Continuity of vector-valued functions
 - Derivatives and Integrals of vector-valued functions
 - Position, velocity, acceleration
 - ¹ Ideal Projectile Motion Equation
 - ¹ Arc Length
 - ¹ Unit Tangent Vector
 - ¹ Curvature, Principal Unit Normal Vector

- Partial Derivatives
 - Functions of several variables
 - Domain, range
 - Interior Points, Boundary Points, Open, Closed
 - Bounded, Unbounded
 - Level Curves, Level Surfaces
 - Graph
 - Limits of Functions of Several Variables
 - ¹ Definition
 - Calculation of Limits
 - Continuous Functions of Several Variables
 - Definition of Partial Derivatives
 - Calculation of Partial Derivatives
 - Chain Rule
 - Mixed Partial Derivatives
 - Directional Derivatives
 - Definition
 - Calculations
 - Gradient
 - Calculation
 - Geometric and Functional Interpretation
 - ¹ Tangent Planes
 - ¹ Differentials and Linearizations
 - Extreme Values and Saddle Points
 - Definitions
 - First Derivative Test
 - Second Derivative Test
 - Calculation of Local and Absolute Extrema

Method of Lagrange Multipliers
Calculations with One Constraint
Calculations with Two Constraints

¹These topics will not be expressly covered on the Final Exam. Though, knowing them may be helpful.