

Name: \_\_\_\_\_

Solution

Section: \_\_\_\_\_

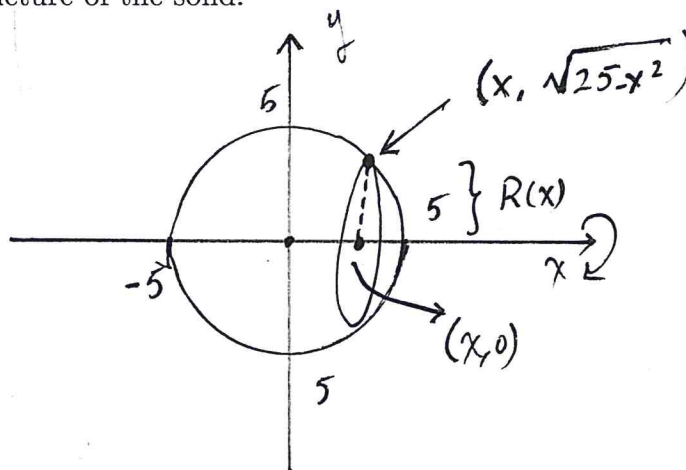
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Clear your desk of everything except pens, pencils and erasers. **Show all your work.**

If you have a question raise your hand and I will come to you.

1. Find the volume of the solid generated by rotating about the  $x$ -axis the region bounded by the curves  $y = \sqrt{25 - x^2}$  and  $y = 0$ .

(a) (4 points) Draw a picture of the solid.



(b) (3 points) Write the formula for the area of a cross-section.

$$\begin{aligned}
 A(x) &= \pi R^2(x) \\
 &= \pi (\sqrt{25-x^2})^2 \\
 &= \pi (25-x^2)
 \end{aligned}$$

(c) (3 points) Set up, **but do not evaluate**, the integral representing the volume of the solid.

$$\begin{aligned}
 V &= \int_{-5}^5 \pi (25-x^2) dx \\
 \text{or } V &= 2 \int_0^5 \pi (25-x^2) dx.
 \end{aligned}$$