

Name: \_\_\_\_\_

PID: \_\_\_\_\_

Section: \_\_\_\_\_

Instructor: \_\_\_\_\_

**DO NOT WRITE BELOW THIS LINE. Go to the next page.**

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Page	Problem	Score	Max Score
1	1		5
	2		5
	3		5
	4		5
	5		5
2	6		5
	7		5
	8		5
	9		5
	10		5
3	11a		8
	11b		4
	12		10
4	13a		6
	13b		6
	13c		6
	13d		4
5	14a		8
	14b		8
	14c		8
6	15		8
	16		8
7	17		8
	18		12
8	19		12
9	20		12
10	21a		2
	21b		2
	21c		2
	21d		2
	21e		2
	21f		4
	21g		4
	21h		4
Total Score			200

Name: \_\_\_\_\_

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Instructor: \_\_\_\_\_

**READ THE FOLLOWING INSTRUCTIONS.**

- **Do not open your exam until told to do so.**
- No calculators, cell phones or any other electronic devices can be used on this exam.
- Clear your desk of everything excepts pens, pencils and erasers.
- If you need scratch paper, use the back of the previous page.
- Without fully opening the exam, check that you have pages 1 through 10.
- Fill in your name, etc. on these first two pages.
- **Show all your work.** Write your answers clearly! Include enough steps for the grader to be able to follow your work. Don't skip limits or equal signs, etc. Include words to clarify your reasoning.
- Do first all of the problems you know how to do immediately. Do not spend too much time on any particular problem. Return to difficult problems later.
- If you have any questions please raise your hand and a proctor will come to you.
- There is no talking allowed during the exam.
- You will be given exactly 120 minutes for this exam.

I have read and understand the above instructions: \_\_\_\_\_

**SIGNATURE****SCORE:**

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**Multiple Choice.** Circle the best answer. No work needed. No partial credit available.

1. Evaluate  $\lim_{x \rightarrow -1} \frac{x^2 + 2x + 1}{x + 1}$

- (a) 1
- (b) -1
- (c) 2
- (d) 0
- (e) None of the above.

2. Evaluate  $\lim_{x \rightarrow -1} \frac{x + 1}{|x + 1|}$

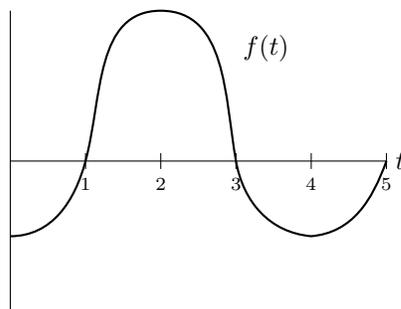
- (a) 1
- (b) -1
- (c) 2
- (d) 0
- (e) None of the above.

3. Find  $c$  so that  $f(x) = \begin{cases} \frac{\sin(3x+x^2)}{x} & \text{if } x \neq 0 \\ c & \text{if } x = 0 \end{cases}$  is continuous.

- (a)  $c = 3$
- (b)  $c = 2$
- (c)  $c = 1$
- (d)  $c = -1$
- (e) None of the above.

4. The graph of  $f(t)$  is shown below. If  $F(x) = \int_0^x f(t) dt$ , for what value of  $x$  is  $F(x)$  an absolute maximum on  $[0, 5]$ ?

- (a)  $x = 0$
- (b)  $x = 1$
- (c)  $x = 2$
- (d)  $x = 3$
- (e) None of the above.



5. Evaluate  $\int x(2x^2 + 1)^3 dx$

- (a)  $\frac{1}{16}(2x^2 + 1)^4 + C$
- (b)  $\frac{1}{12}(2x^2 + 1)^4 + C$
- (c)  $\frac{1}{8}(2x^2 + 1)^4 + C$
- (d)  $\frac{1}{4}(2x^2 + 1)^4 + C$
- (e) None of the above.

**Fill in the Blanks.** No work needed. Only possible scores given are 0, 3, and 5.

6. If  $f(x) = x^2 \sin x$  then  $f'(x) =$  \_\_\_\_\_

7. The vertical asymptote(s) of  $f(x) = \frac{1-x}{x+2}$  are \_\_\_\_\_. The horizontal asymptote(s) of  $f(x)$  are \_\_\_\_\_.

8.  $\frac{d}{dt} \left( \frac{(t + \tan t)^2}{\sqrt{t}} \right) =$  \_\_\_\_\_

9. A function which satisfies  $y'(x) = 4x$  and  $y(1) = 5$  is given by  $y(x) =$  \_\_\_\_\_

10. Let  $f$  and  $g$  be differentiable functions such that

$$\begin{array}{lll} f(0) = 2 & f'(0) = 3 & f'(2) = 4 \\ g(0) = 2 & g'(0) = -1 & g'(2) = 5 \end{array}$$

If  $h(x) = g(f(x))$  then  $h'(0) =$  \_\_\_\_\_

**Extra Work Space.**

**Standard Response Questions.** Show all work to receive credit. Please put your final answer in the **BOX**.

11. (8+4=12 points) Throughout this problem  $y$  is defined implicitly as a function of  $x$ .

(a) Find the slope of the tangent line to the curve  $y^2 + 7x = x^2y + 9$  at the point  $(1, 2)$ .

**Answer:**

(b) Write the equation of the tangent line to the curve at the point  $(1, 2)$ .

**Answer:**

$y =$

12. (10 points) Use the *definition* of the derivative *as a limit* to calculate  $f'(x)$  for

$f(x) = \frac{2}{x-3}$ . (There will be no credit for other methods.)

**Answer:**

$f'(x) =$

13. (6+6+6+4=22 points) Let  $f(x) = x + 2 \cos(x)$  on the interval  $[0, 2\pi]$ .

- (a) Find the intervals within  $[0, 2\pi]$  on which  $f$  is increasing and the intervals on which  $f$  is decreasing.

**Answer:**

$f$  is increasing on:

$f$  is decreasing on:

- (b) Find the intervals within  $[0, 2\pi]$  on which  $f$  is concave up and the intervals on which  $f$  is concave down.

**Answer:**

$f$  is concave up on:

$f$  is concave down on:

- (c) Indicate the  $y$ -intercept, any local maxes/mins, and inflection points.

**Answer:**

$f$  has  $y$ -intercept at:

$(x, y) =$

$f$  has local max(s) at:

$x =$

$f$  has local min(s) at:

$x =$

$f$  has inflection point(s) at:

$x =$

- (d) Locate the absolute maximum of  $f$  on  $[0, 2\pi]$ .

**Answer:**

$f$  has an absolute max at:

$x =$

14. (8+8+8=24 points) Evaluate the following integrals:

$$(a) \int \frac{x^3}{\sqrt{1+2x^4}} dx$$

**Answer:**

$$(b) \int \frac{\sec\left(\frac{x}{2}\right) \tan\left(\frac{x}{2}\right)}{\sqrt{\sec\left(\frac{x}{2}\right)}} dx$$

**Answer:**

$$(c) \int_8^{11} x\sqrt{x-7} dx$$

**Answer:**

15. (8 points) Use the Fundamental Theorem of Calculus to find the derivative of

$$F(x) = \int_{\pi}^{\sqrt{x}} \frac{2 \sin(t^2) - 1}{\sqrt{t^4 + 1}} dt$$

**Answer:**

$$F'(x) =$$

16. (8 points) Estimate  $\int_1^4 \frac{2x-1}{\sqrt{x}} dx$  using areas of 3 rectangles of equal width, with heights of the rectangles determined by the height of the curve at left endpoints (Do not simplify).

**Answer:**

17. (8 points) Use a linear approximation to estimate  $\sqrt[3]{26}$ .

**Hint:** Is 26 close to a number whose cube root is well-known?

**Answer:**

$$\sqrt[3]{26} \approx$$

18. (12 points) Find the area of the region enclosed by the graphs of the equations  $y = 2x^2 + x - 2$  and  $y = x^2 - x + 1$ .

**Answer:**

$$\text{Area} =$$

19. (12 points) The top of a 13 foot ladder, leaning against a vertical wall, is slipping down the wall at the rate of 2 feet per second. How fast is the bottom of the ladder sliding along the ground away from the wall when the bottom of the ladder is 5 feet away from the base of the wall?

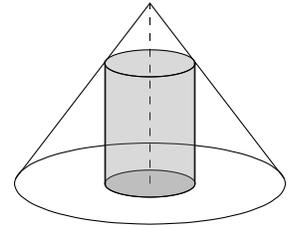
**Answer:**

ft/s

20. (12 points) A cylinder is inscribed in a right circular cone of height 4 inches and radius (at the base) equal to 3 inches. What are the dimensions of such a cylinder that has maximum volume?

**You MUST verify that you have found the maximum.**

**Hint:** Recall the formula for volume of a cylinder:  $V = \pi r^2 h$



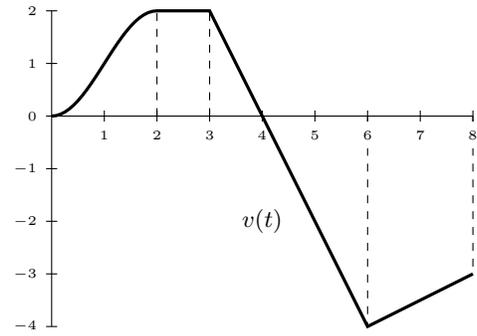
**Answer:**

height =

radius =

21. (2+2+2+2+2+4+4+4=22 points)

The graph to the right shows the velocity  $v(t)$  in meters per second of a particle moving on a horizontal coordinate line, for  $t$  in seconds within the closed interval  $[0, 8]$ .



(a) When is the particle moving forward?

**Answer:**

$t \in$   $s$

(b) When is the particle's speed decreasing?

**Answer:**

$t \in$   $s$

(c) When is the particle's acceleration positive?

**Answer:**

$t \in$   $s$

(d) When is the particle's acceleration the greatest?

**Answer:**

$t =$   $s$

(e) When does the particle move at its greatest speed?

**Answer:**

$t =$   $s$

(f) What is the change in the particle's position from  $t = 2$  to  $t = 6$ ?

**Answer:**

Change in position =  $m$

(g) What is the total distance the particle travels from  $t = 2$  to  $t = 6$ ?

**Answer:**

Distance traveled =  $m$

(h) If the particle is at the origin at  $t = 2$  use linear approximation to estimate its position at  $t = 3/2$

**Answer:**

$s(3/2) \approx$   $m$