

For Monday review triple integrals in section 15.4, and read about cylindrical and spherical coordinates in section 15.6.

1) Find the area inside the ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

by integrating  $f(x, y) = 1$  over that region. Use the substitution  $x = au$ ,  $y = bv$  to simplify the integral first.

2) Find the Jacobian of the transformation  $x = u$ ,  $y = uv$  and sketch the region  $1 \leq x, y \leq 2$  in the  $(u, v)$ -plane. Use this to evaluate the integral:

$$\int_1^2 \int_1^2 \frac{y}{x} dy dx$$

by making a substitution.

3) Evaluate the integral

$$\int \int_{\mathcal{R}} (2x^2 - xy - y^2) dx dy$$

where  $\mathcal{R}$  is the region in the first quadrant bounded by  $y = -2x + 4$ ,  $y = -2x + 7$ ,  $y = x - 2$ , and  $y = x + 1$ . (Hint: try factoring the quadratic you are integrating and then using a substitution  $u = ax + by$ ,  $v = cx + dy$ ).