Worksheet 18 - Stokes' Theorem

1. Find the circulation of the field:

$$\vec{F} = \left\langle y, xz, x^2 \right\rangle$$

around the curve C, where C is the boundary of the triangle cut from 4x + y + z = 4 by the first octant, counterclockwise when viewed from above.

2. Evaluate:

$$\iint_{S} \nabla \times (3y\vec{i}) \cdot \vec{n} \, d\sigma,$$

where S is the hemisphere $x^2 + y^2 + z^2 = 1$, $z \ge 0$.

3. Compute the flux of the curl of the field:

$$\vec{F} = \langle 4y, 5 - 5x, z^2 - 2 \rangle$$

across the surface S:

$$S \ : \ \vec{r}(\phi,\theta) = \left\langle \sqrt{5}\sin\phi\cos\theta, \ \sqrt{5}\sin\phi\sin\theta, \ \sqrt{5}\cos\phi \right\rangle, \ 0 \le \phi \le \frac{\pi}{2}, \ 0 \le \theta \le 2\pi,$$

in the direction of the outward unit normal.