

**Final Exam Review: Worksheet 3**

1. Find  $k$  such that the function  $f$  is continuous everywhere:

$$f(x) = \begin{cases} x^2 + 2x, & \text{if } x \leq k \\ 2x^2 + 2x - 1, & \text{if } x > k. \end{cases}$$

2. Find  $k$  such that the function  $f$  is continuous everywhere:

$$f(x) = \begin{cases} x^2 + x - 2k, & \text{if } x \leq 2 \\ 6x + k, & \text{if } x > 2. \end{cases}$$

3. Find  $k$  such that  $y = -4x + k$  is a tangent line to the graph of  $f(x) = x^3 + 3x^2 - x + 1$ .  
4. Find  $k$  such that  $y = 2x + 6$  is a tangent line to the graph of  $f(x) = x^2 - 2x + k$  at the point where  $x = 2$ .  
5. Find  $k$  such that

$$\int_k^{k+1} (2x + 1) dx = 2.$$

6. Find  $k$  such that the average value of

$$f(x) = \frac{1}{\sqrt{x}} + 2x - k$$

on the interval  $[0, k]$  is equal to 8.

7. Find  $k$  such that

$$\int_1^2 \frac{(x+k)(x-k)}{2x^2} dx = 0.$$

8. Find  $k$  such that

$$\int_{-k}^k \frac{(x-1)(x+3)}{x^4} dx = 0.$$

9. Find all values  $c$  which satisfy the conclusion of the Mean Value Theorem for

$$f(x) = x^3 + 2x^2 - x$$

on the interval  $[-1, 2]$ .

10. Let  $f$  be a function with first derivative given by

$$f'(x) = \frac{2x^2 - 5}{x^2}$$

for all  $x > 0$ . Given that  $f(1) = 7$  and  $f(5) = 11$ , what value  $c \in (1, 5)$  satisfies the conclusions of the Mean Value Theorem for  $f$  on the interval  $[1, 5]$ ?

11. Suppose  $f$  is continuous on  $[0, 2]$  and has values:

$x$		0		1		2
$f(x)$		1		$k$		2

The equation  $f(x) = \frac{1}{2}$  must have at least two solutions in the interval  $[0, 2]$  if  $k$  is:

- a). 0; b).  $1/2$ ; c). 1; d). 2; e). 3.

12. Selected values of a continuous function  $g$  are below:

$x$		0		2		5		9		11
$g(x)$		1		2.8		1.7		1		3.4

For  $0 \leq x \leq 11$ , what is the minimum number of times  $g(x) = 2$ ?

- a). One; b). Two; c). Three; d). Four; e). Five.