

Consider the function

$$f(x) = \frac{1}{x}$$

1). Find a power series representation of the form

$$f(x) = \sum_{n=0}^{\infty} c_n (x-2)^n$$

by using the geometric series. (+ Interval of conv.)

Hint: Write  $f$  as:  $f(x) = \frac{1}{x} = \frac{1}{2 + (x-2)}$

2). Now use Taylor series formula

$$f(x) = \sum_{n=0}^{\infty} \frac{f^{(n)}(a)}{n!} (x-a)^n$$

to obtain the Taylor series of  $f(x) = \frac{1}{x}$  about  $x=2$ .