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## Areas between curves are computed with appropriate integrals

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**Theorem 2** Let f(x), g(x) be continuous functions in [a, b]. If  $f(x) \ge g(x)$  with  $x \in [a, b]$ , then the area between their graphs is

$$A = \int_{a}^{b} [f(x) - g(x)] \, dx.$$

The hypothesis that  $f(x) \ge g(x)$  is not needed

**Theorem 3** Let f(x), g(x) be continuous functions in [a, b]. Then the area between their graphs is

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$$A = \int_a^b |f(x) - g(x)| \, dx.$$

Just replace f(x) - g(x) by its absolute value |f(x) - g(x)|.

## Volumes are computed integrating the area function

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**Theorem 4** Let S be 3-dimensional body that along the x-axis lies in [a, b]. Let A(x) be the cross section area of S perpendicular to the x-axis evaluated at x. Then, the volume of S is

$$V = \int_{a}^{b} A(x) \, dx.$$

## The volume of solids of revolution are computed with a particular case of the previous formula

- Given a function f(x) with  $x \in [a, b]$ , construct a solid of revolution rotating the graph of f around the *x*-axis.
- The sections perpendicular to the x-axis of such a solid are precisely disks or radius |f(x)|.
- Then, the area of cross sections for such a solid is  $A(x) = \pi [f(x)]^2$ .

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The volume of solids of revolution are computed with a particular case of the previous formula

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**Theorem 5** Let S be 3-dimensional solid of revolution obtained rotating the graph of f(x) for  $x \in [a, b]$  along the x-axis. Then, the volume of S is

$$V = \pi \int_a^b [f(x)]^2 \, dx.$$