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TA Name: $\qquad$ Section Time: $\qquad$
Math 20B.
Midterm Exam 1
January 28, 2004

You may use one page of notes, but no other assistance on this exam.
Read each question carefully, answer each question completely, and show all of your work. Write your solutions clearly and legibly; no credit will be given for illegible solutions. If any question is not clear, ask for clarification.

1. (4 points) Find the area of the region bounded by the graphs of $y=x^{2}$ and $y=2 x^{2}+3 x$.

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2. (4 points) Find the area enclosed by the polar curve $r=3(1+\cos \theta)$.

3. A vehicle travels along a line so that its velocity at time $t$ is $v(t)=2 t-4$ feet per second.
(a) (2 points) Find the displacement (net distance traveled) of the vehicle from $t=0$ to $t=4$ seconds.
(b) (4 points) Find the total distance traveled by the vehicle from $t=0$ to $t=4$ seconds.
4. (4 points) Find the cube roots of $27 i$ and express them in polar form.
5. Evaluate the following integrals.
(a) (4 points) $\int 5 x \sin \left(x^{2}\right) d x$
(b) (4 points) $\int_{1}^{2} x^{2} \sqrt{x-1} d x$
6. (4 points) A spherical water tank of radius $r$ feet is filled to a depth $h$ feet. Find the volume of water in the tank.

