

Build-your-own formula sheet.

Algebraic

- ★ $a^2 - b^2 = (a - b)(a + b)$, $(\sqrt{A} - \sqrt{B})(\sqrt{A} + \sqrt{B}) = A - B$
- $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$
- Quadratic Formula: $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Geometric

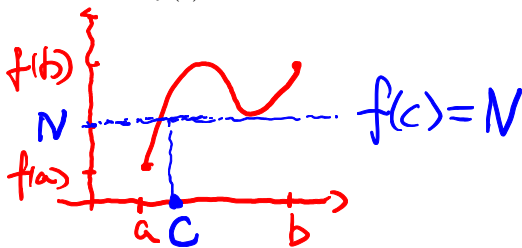
- Area of Circle: πr^2
- Circumference of Circle: $2\pi r$
- Circle with center (h, k) and radius r :
 $(x - h)^2 + (y - k)^2 = r^2$
- Distance from (x_1, y_1) to (x_2, y_2) :
 $\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$

- Area of Triangle: $\frac{1}{2}bh$
- $\sin \theta = \frac{\text{opposite leg}}{\text{hypotenuse}}$
- $\cos \theta = \frac{\text{adjacent leg}}{\text{hypotenuse}}$
- $\tan \theta = \frac{\text{opposite leg}}{\text{adjacent leg}}$
- If $\triangle ABC$ is similar to $\triangle DEF$ then
 $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$

- Volume of Sphere: $\frac{4}{3}\pi r^3$
- Surface Area of Sphere: $4\pi r^2$
- Volume of Cylinder/Prism: (height)(area of base)
- Volume of Cone/Pyramid: $\frac{1}{3}$ (height)(area of base)

Theorems

- (IVT) If f is continuous on $[a, b]$, $f(a) \neq f(b)$, and N is between $f(a)$ and $f(b)$ then there exists $c \in (a, b)$ that satisfies $f(c) = N$.



- (Squeeze Thm) Suppose $f(x) \leq g(x) \leq h(x)$
and $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} h(x) = L$
Then $\lim_{x \rightarrow a} g(x) = L$.

Limits

- $\lim_{x \rightarrow a} f(x)$ exists if and only if $\lim_{x \rightarrow a^-} f(x) = \lim_{x \rightarrow a^+} f(x)$
- $\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$
- $\lim_{\theta \rightarrow 0} \frac{1 - \cos \theta}{\theta} = 0$

Derivatives

- $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$
- $(\cot x)' = -\csc^2 x$
- $(\csc x)' = -\csc x \cdot \cot x$

Trigonometric

- $\sin^2 \theta + \cos^2 \theta = 1$
- $\sin(2\theta) = 2 \sin \theta \cos \theta$
- $\cos(2\theta) = \cos^2 \theta - \sin^2 \theta$
 $= 1 - 2 \sin^2 \theta$
 $= 2 \cos^2 \theta - 1$
- Table of Trig Values

x	0	$\pi/6$	$\pi/4$	$\pi/3$	$\pi/2$
$\sin(x)$	0	1/2	$\sqrt{2}/2$	$\sqrt{3}/2$	1
$\cos(x)$	1	$\sqrt{3}/2$	$\sqrt{2}/2$	1/2	0
$\tan(x)$	0	$\sqrt{3}/3$	1	$\sqrt{3}$	DNE $\pm \infty$

More derivatives:

$$(\text{const})' = 0, (kx + b)' = k$$

$$(x^n)' = n \cdot x^{n-1}$$

$$(f \pm g)' = f' \pm g', (c \cdot f)' = c \cdot f'$$

$$\left(\frac{f}{c}\right)' = \frac{f'}{c}$$

$$(f \cdot g)' = f' \cdot g + f \cdot g'$$

$$\left(\frac{f}{g}\right)' = \frac{f' \cdot g - f \cdot g'}{g^2}$$

$$\bullet (\sin x)' = \cos x, (\cos x)' = -\sin x$$

$$(\tan x)' = \sec^2 x, (\sec x)' = \tan x \cdot \sec x$$

$$\bullet [f(g(x))]' = f'(g(x)) \cdot g'(x)$$

• tangent line equation at $x=a$

$$y = f'(a) \cdot (x-a) + f(a)$$

$$\bullet |x| = \begin{cases} x, & x \geq 0 \\ -x, & x < 0 \end{cases}$$

$$\frac{1}{x} = x^{-1}, \sqrt{x} = x^{\frac{1}{2}}$$