

**Math 421 / Homework 8.1**

- # 3 Show that the equality in the Cauchy-Schwarz Inequality holds if and only if  $\mathbf{x} = 0$ ,  $\mathbf{y} = 0$ , or  $\mathbf{x}$  is parallel to  $\mathbf{y}$ .
- # 4(b) If  $\theta \in [0, \pi]$  is the angle between two nonzero vectors  $\mathbf{a}$  and  $\mathbf{b}$  in  $\mathbf{R}^n$ , show that  $\mathbf{a}$  and  $\mathbf{b}$  are parallel if and only if  $\theta = 0$  or  $\pi$ , and that  $\mathbf{a}$  and  $\mathbf{b}$  are orthogonal if and only if  $\theta = \pi/2$ .
- # 9 Suppose that  $(a_k)$  and  $(b_k)$  are sequences of real numbers which satisfy

$$\sum_{k=1}^{\infty} a_k^2 < \infty \quad \text{and} \quad \sum_{k=1}^{\infty} b_k^2 < \infty.$$

Prove that the infinite series  $\sum_{k=1}^{\infty} a_k b_k$  converges absolutely.