## Math 254H

Recall that  $F : \mathbb{R}^n \to \mathbb{R}^m$  has Jacobian derivative matrix [DF] with m rows, n columns.

**1.** Consider a function  $\mathbf{c} : \mathbb{R} \to \mathbb{R}^2$ , tracing the curve  $\mathbf{c}(t) = (x(t), y(t))$ . Write the derivative matrix  $[D\mathbf{c}_t]$  in terms of the coordinate functions x(t) and y(t).

**2.** Consider a function  $f : \mathbb{R}^2 \to \mathbb{R}$ . Write the derivative matrix  $[Df_{(x,y)}]$ .

**3.** Use the Chain Rule to compute the derivative matrix of the composite function  $F : \mathbb{R}^2 \to \mathbb{R}^2$  given by  $F(u, v) = \mathbf{c}(f(u, v))$ .