\LaTeX Graphics with PSTricks

This presentation is also available online. Please visit my home page and follow the links.

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1. Resources

(a) ImageMagick is a collection of (free) image manipulation tools. You can find out more by visiting

http://www.imagemagick.com

(b) The \LaTeX Graphics Companion.
   - Paperback: 608 pages
   - Publisher: Addison-Wesley Pub Co; 1st edition (April 15, 1997)
   - ISBN: 0201854694

(c) The \LaTeX Graphics Companion (2nd Edition).
   - Paperback: 976 pages
   - Publisher: Addison-Wesley Professional; 2 edition (August 12, 2007)
   - ISBN: 0321508920

(d) PSTricks: Graphics and PostScript for \TeX and \LaTeX.
   - Paperback: 912 pages
   - Publisher: UIT Cambridge Ltd. (September 1, 2011)
   - ISBN: 1906860130

(e) The PSTricks web site.

https://www.tug.org/PSTricks

(f) PostScript(R) Language Tutorial and Cookbook (also called the “The Blue Book”)
   - Paperback: 256 pages
   - Publisher: Addison-Wesley Professional (January 1, 1985)
   - ISBN: 0201101793

2. PSTricks
(a) We start with some examples.

Figure 1: Graphing simple functions.

Figure 2: Graphing with some fancy effects.
\[ r = 1 + 2 \sin \theta \]

**Figure 3: Polar Graphs**

**Figure 4: Area between two curves.**
Figure 5: A pair of vectors

Figure 6: Vector addition with a grid.
Figure 7: Polar Grid

Figure 8: Sketching a cylinder.
Figure 9: Position Vectors

Figure 10: Level Curves
Figure 11: Polar Area

Figure 12: A Tangent Line
Figure 13: Lagrange Multipliers

\[ xy = c \]

Values of \( c \):
- \( c = 0.01 \)
- \( c = 0.025 \)
- \( c = 0.05 \)
- \( c = 0.075 \)
- \( c = 0.1 \)
- \( c = 0.11 \)
- \( c = 0.125 \)
Figure 14: Exposed Solid
Figure 15: Surface Integrals

Figure 16: Distorted Surface
Figure 17: Fractals
Figure 18: Lens Effects

Figure 19: Vector Field
3. PSTricks

To use PSTricks you must include the following lines in the preamble of your document.

\begin{verbatim}
\usepackage{pst-eucl}
\usepackage{calc}
\usepackage{pst-3dplot}\
\usepackage{pst-grad}
\usepackage{pst-plot,pst-math,pstricks-add}\
\usepackage{pst-all}\
\%\RequirePackage{pst-xkey}
\end{verbatim}

We should mention that there have been some incompatibilities between the pstcol package (used by PSTricks) and the graphics packages mentioned above.

Using colors with PSTricks is similar to what has already been discussed. The real power of the PSTricks package is the ability to create graphics using L\LaTeX-like syntax.
PSTricks provides users with the capability to draw using the familiar syntax of \LaTeX.

\begin{verbatim}
\psline[linecolor=blue,linewidth=1.25pt](-3,1)(2,2)
\end{verbatim}

The previous example might be easier to understand if we include more detail in the sketch. Thus

\begin{verbatim}
\showgrid
\psline[linecolor=blue,linewidth=1.25pt,arrowscale=2]{->}(-3,1)(2,2)
\end{verbatim}

\begin{verbatim}
\newpsobject{showgrid}{psgrid}{%
    gridlabels=0pt%,
    ,griddots=0%
    ,gridwidth=0.5pt%
    ,gridcolor=gray%
    ,subgriddiv=0%
    ,subgridwidth=0.25pt%
    ,subgridcolor=red}
\end{verbatim}
(b) Basic Graphics Objects

Here’s a curve. Notice that the points used can be turned on (as shown) or off.

\begin{pspicture}(\xmin,\ymin)(\xmax,\ymax)
  \showgrid
  \pscurve[linecolor=red,linewidth=1.5pt,showpoints=true]\
  (\xmin,1)(0,2)(3,1)(\xmax,\ymax)
\end{pspicture}

where the values \texttt{\xmin}, \texttt{\ymin}, etc. have been defined previously as

\begin{verbatim}
def\xmin{-6}\def\xmax{6}
def\ymin{-6}\def\ymax{6}
\end{verbatim}
We begin by setting the default unit(s) in PSTricks using the command \psset{unit=1cm}. This is actually the default value.

\begin{pspicture}(\xmin,\ymin)(\xmax,\ymax)
\showgrid
\pscurve[linecolor=red,linewidth=1.5pt,showpoints=true]\
(\xmin,1)(0,2)(3,1)(\xmax,\ymax)
\psbezier[style=myCurveStyle,linecolor=green]{-}\
(-4,1)(-2,3)(1,-4)(5,5)
\end{pspicture}

There are built-in shapes

\begin{pspicture}(\xmin,\ymin)(\xmax,\ymax)
\showgrid
\psellipse[linecolor=blue,linewidth=1.5pt]\
(1,0)(1,1.5)
\psdots[linecolor=red,linewidth=1.25pt](0,0)
\SpecialCoor
\uput{6pt}[180](0,0){\$$(0,0)\$$}
\NormalCoor
\end{pspicture}
Here is a circle centered at \((-2, -1)\) of radius 2.

\begin{pspicture}(\xmin,\ymin)(\xmax,\ymax)
\showgrid\pscircle*[linecolor=red,linewidth=1.5pt](-2,-1){2}
\end{pspicture}

Here is the same object filled-in and clipped.

\begin{pspicture}(\xmin,\ymin)(\xmax,\ymax)
\showgrid\psclip{myframe(\xmin,\ymin)(\xmax,\ymax)}
\pscircle*[linecolor=red,linewidth=1.5pt](-2,-1){2}
\endpsclip\pswedge*[linecolor=white](-2,-1){15}{105}
\end{pspicture}
Finally, we plot some functions. To do this we’ll use some custom macros that give the user better control over the coordinate system.

```latex
\begin{pspicture}(\xmin,\ymin)(\xmax,\ymax)
  \showgrid
  \pstVerb{%
    /f@ {dup mul} def \% x^2
  }
  \myaxes{<->}(0,0)(\xmin,\ymin)(\xmax,\ymax)
  \xTickMarks{\xmin}{\xmax}{1}
  \yTickMarks{\ymin}{\ymax}{5}
  \myframe(\xmin,\ymin)(\xmax,\ymax)
  \psplot[style=myPlotStyle]
  {\xmin}{\xmax}{x f@}
  \uput{6pt}[0]{!3 dup f@}{$y=x^2$}
\end{pspicture}
```
And again, using better grid controls.
Here’s something useful for integration theory. Use the sketch to estimate the integral below.

\[ \int_{2}^{5} \frac{1}{x} \, dx \]
Here is the code

```
def\xmin{0}\def\xmax{6}
def\ymin{0}\def\ymax{1}
def\dommin{\xmin}\def\dommax{\xmax}
\VR{3in}{2.5in}

\newpsobject{newgrid}{psgrid}{%
gridlabels=0pt%
,griddots=0%
,gridwidth=0.5pt%
,gridcolor=gray%
,subgriddiv=4%
,subgridwidth=0.25pt%
,subgridcolor=red%
}\begin{pspicture}(\xmin,\ymin)(\xmax,\ymax)
\newgrid
%%%%%%%%%%%%%%%%%%%%
%% Axes and Ticks %%
%%%%%%%%%%%%%%%%%%%%
\SpecialCoor
%% Labels go here
\rput[lr]{(!\xmax\space\xmax\space\xmin\space sub 15 di v sub
\ymax\space\ymax\space\ymin\space sub 25 div sub){$y=\frac{1}{x}$}}
\NormalCoor
\myaxes{<->}(0,0)(\xmin,\ymin)(\xmax,\ymax)
%% Change these as needed. #1 - start, #2 - end, #3 - increment
\xTickMarks{\xmin}{\xmax}{1}
\yTickMarks{\ymin}{\ymax}{1}
\psclip{\psframe(\xmin,\ymin)(\xmax,\ymax)}
%% Graphing directives go here, e.g.,
\psplot[style=myPlotStyle]
{0.1}{\xmax}{1 x div}
\endpsclip
\SpecialCoor
\psline[fillstyle=crosshatch]{-}((3,0)(3.5,0)(!3.5 1 3
div)(!3 1 3 div)(3,0)
\psline[fillstyle=crosshatch]{-}((3.5,0)(4,0)(!4 1 3.5
div)(!3.5 1 3.5 div)(3.5,0)
\psline[fillstyle=crosshatch]{-}((4,0)(4.5,0)(!4.5 1 4
div)(!4 1 4 div)(4,0)
\psline[fillstyle=crosshatch]{-}((4.5,0)(5,0)(!5 1 4.5
div)(!4.5 1 4.5 div)(4.5,0)
\NormalCoor
\end{pspicture}
```
(c) Plotting Data from a File

Suppose that you wish to plot the following data.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>0,</td>
<td>0</td>
</tr>
<tr>
<td>0.0628,</td>
<td>0.06279</td>
</tr>
<tr>
<td>0.1256,</td>
<td>0.12533</td>
</tr>
<tr>
<td>...</td>
<td>...</td>
</tr>
</tbody>
</table>

The following code does the trick.

```latex
\begin{pspicture}(\xmin,\ymin)(\xmax,\ymax)
\showgrid
%% Axes and Ticks %%
\myaxes{<->}(0,0)(\xmin,\ymin)(\xmax,\ymax)
%% Graphical Objects %%
\psclip{\myframe(\xmin,\ymin)(\xmax,\ymax)}
\fileplot{plotData.txt}
\endpsclip
\SpecialCoor
\rput[lt](!\xmax\space\xmin\space sub 15 div \ymax\space\ymax\space\ymin\space sub 25 div sub){$y=\sin x$}
\NormalCoor
\end{pspicture}
```
4. Several examples from geometry.
5. A few exotic tricks.

(a) A vector field.
(b) An ice-cream cone.
(c) A level surface.

\[ f(x, y, z) = c \]
The equation of a sphere with radius $r$ centered at the origin is

$$x^2 + y^2 + z^2 = r^2$$
Figure 22: Brownian Motion

Figure 23: Not Sure What to Call This
Figure 24: Tessellations?
Figure 25: $\pi$ Spiral
Transparency Effects

The sketch below shows the infinite plane $x = 0$.

In a similar manner one can sketch the graphs of the equations $y = 0$ and $z = 0$.

Notice that these three planes break up three-space into eight octants. The first octant coincides with positive $x,y$ and $z$-coordinates and is three-dimensional analogue of quadrant I in the plane.
A Saddle Point
Example 1. A Familiar Curve

Find the areas of the shaded regions.

\[ r_1 = 2 \cos \theta - \sin \theta \]
\[ r_2 = \cos \theta \]

We first need to find the polar coordinates of point of intersection, \( P \). Setting \( r_1 = r_2 \) and solving we see that \( \theta = \pi/4 \). It follows that the area of green portion of the shaded region is given by

\[ A_G = \frac{1}{2} \int_0^{\pi/4} (r_1^2 - r_2^2) \, d\theta \]

It follows that

\[
A_G = \frac{1}{2} \int_0^{\pi/4} \sin^2 \theta + 3 \cos^2 \theta - 4 \sin \theta \cos \theta \, d\theta \\
= \frac{1}{2} \int_0^{\pi/4} 1 + 2 \cos^2 \theta - 2 \sin 2\theta \, d\theta \\
= \frac{1}{2} \int_0^{\pi/4} 2 + \cos 2\theta - 2 \sin 2\theta \, d\theta \\
= \frac{1}{4} (4\theta + \sin 2\theta + 2 \cos 2\theta) \bigg|_0^{\pi/4} \\
= \frac{1}{4} \{ (\pi + 1 + 0) - (0 + 0 + 2) \} = \frac{\pi - 1}{4}
\]

Notice that

\[ A_G + A_B = \frac{1}{2} \int_0^{\arctan 2} r_1^2 \, d\theta \]

(Compare this last equation to the gas tank problem.)

Finally, can you find \( A_Y \)?
Definition. The Gamma Function

\[ \Gamma(x) = \int_0^\infty t^{x-1}e^{-t}\,dt \quad (1) \]

Here the (improper) integral converges absolutely for all \( x \in \mathbb{R} \) except for the non-positive integers. In fact, the Gamma function can be extended throughout the complex plane (again, except for the non-positive integers).

Observe that

\[ \Gamma(1) = \int_0^\infty t^0e^{-t}\,dt \]
\[ = \frac{-1}{e^t} \bigg|_0^\infty = 0 - (-1) = 1 \]

and for positive integers \( n \), integration by parts yields the recursive relation

\[ \Gamma(n + 1) = \int_0^\infty t^n e^{-t}\,dt \]
\[ = -t^n e^{-t} \bigg|_0^\infty + n \int_0^\infty t^{n-1} e^{-t}\,dt \]
\[ = 0 + n \Gamma(n) \]

and Euler had found his extension. That is, for each nonnegative integer \( n \), he could now define the factorial by

\[ n! = \Gamma(n + 1) \quad (2) \]
Sketch the curve given by the equation below in polar coordinates.

\[ r_1 = f(\theta) = 2 \cos \theta - \sin \theta, \quad 0 \leq \theta \leq \pi \quad (3) \]

This busy sketch requires some explanation. Recall that the given (polar) equation defines a circle of radius \( \sqrt{5}/2 \) centered at \((1, -1/2)\). The blue part of circle identifies that portion of polar equation \( r_1 = 2 \cos \theta - \sin \theta \), \( 0 \leq \theta \leq \arctan 2 \), i.e., when \( r_1 \geq 0 \). The red part identifies the part of the curve for \( \arctan 2 \leq \theta \leq \pi \), i.e., when \( r_1 < 0 \).

The yellow portion is actually the sketch of the curve

\[ r_2 = |f(\theta)|, \quad \arctan 2 \leq \theta \leq \pi \quad (4) \]

The vectors (arrows) trace out the curve \( r_2 \) for \( 0 \leq \theta \leq 2\pi \). Notice that the equation in (4) yields two circles which are symmetric about the line \( y = 2x \) (shown in green).