

1. (3 points) Let $f(x) = \sin\left(\frac{\pi x}{6}\right) - x^2$. Find the average rate of change in the function between $x = 1$ and $x = 3$. *Your answer should be a number.*

Solution:

$$f(3) = \sin\left(\frac{3\pi}{6}\right) - (3)^2 = -8$$

and

$$f(1) = \sin\left(\frac{\pi}{6}\right) - (1)^2 = -1/2$$

It follows that

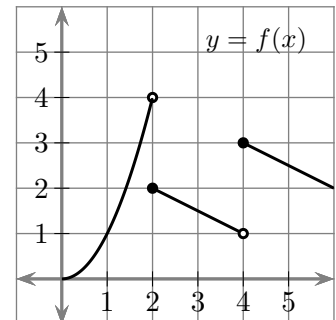
$$f_{\text{avg}} = \frac{f(3) - f(1)}{3 - 1} = \frac{-15}{4}$$

2. (4 points) Let $y = f(x)$ as shown. Compute the limits that follow (or explain why they do not exist).

(a) $\lim_{x \rightarrow 2} f(x) = \text{DNE}$ since the LHL \neq RHL

(b) $\lim_{x \rightarrow 4^-} f(x) = 1$

A few comments: Notice that $\lim_{x \rightarrow 4^+} f(x) = 3$ so that $\lim_{x \rightarrow 4} f(x) = \text{DNE}$.



3. (3 points) Evaluate the limit below.

$$\lim_{x \rightarrow 5^-} \frac{|x - 5|}{x - 5} =$$

Can the Quotient Rule (of the Limit Laws) be used for the above limit? No

Solution:

Since $x < 5$ we have

$$\lim_{x \rightarrow 5^-} \frac{|x - 5|}{x - 5} = \lim_{x \rightarrow 5^-} \frac{-(x - 5)}{x - 5} = \lim_{x \rightarrow 5^-} -1 = -1$$