$\begin{array}{c} {\rm Math~20A} \\ {\rm Second~Midterm~Exam.~November~19,~2002} \\ {\rm VERSION~2} \end{array}$

Instructions: Fifty-five minutes. No books or notes; graphing calculators without symbolic manipulation programs are permitted. Do all 5 problems in your blue book. Show all work; unsubstantiated answers will not receive credit. Turn in your exam sheet with your blue book.

- 1. (20 points) Differentiate the following functions:
 - (a) $x^2 \ln x$.
 - (b) $\sin\left(e^{5x^3}\right)$.
- 2. (20 points) Use differentials to estimate the volume of paint required to cover the surface of a cube, with sides of length 10 inches, with a 0.015 inch thick coat of paint.
- 3. (20 points) If a sphere of ice melts so that its surface area decreases at a rate of 1 cm²/min, find the rate at which the diameter decreases when the diameter is 30 cm. (Recall that the surface area of a sphere of radius r is $4\pi r^2$.)
- 4. (20 points) Let f be a continuous function on [1,7], differentiable on (1,7), with f(1) = 0 and $f'(x) \ge 1$ for 1 < x < 7. Find the smallest possible value of f(7). Justify your answer.
- 5. (40 points) Let $f(x) = xe^{-2x}$.
 - (a) Find the local maxima and local minima of f, if any.
 - (b) Find the intervals on which f is increasing and the intervals on which f is decreasing.
 - (c) Find the inflection points of the graph of f.
 - (d) Find the intervals on which the graph of f is concave up and the intervals on which the graph of f is concave down.